

KEY

For details, see  
Google Classroom  
solutions  
for  
1998  
exam.

## 1998 Practice Exam (No Calculator)

25. What is the area of the region between the graphs of  $y = x^2$  and  $y = -x$  from  $x = 0$  to  $x = 2$ ?

(A)  $\frac{2}{3}$

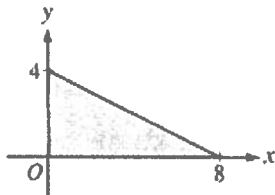
(B)  $\frac{8}{3}$

(C) 4

(D)  $\frac{14}{3}$

(E)  $\frac{16}{3}$

## 1998 Practice Exam (Calculator OK)

86. The base of a solid is a region in the first quadrant bounded by the  $x$ -axis, the  $y$ -axis, and the line  $x + 2y = 8$ , as shown in the figure above. If cross sections of the solid perpendicular to the  $x$ -axis are semicircles, what is the volume of the solid?

(A) 12.566

(B) 14.661

(C) 16.755

(D) 67.021

(E) 134.041

## 1998 Practice Exam

(Calculator OK)

1. Let  $R$  be the region bounded by the  $x$ -axis, the graph of  $y = \sqrt{x}$ , and the line  $x = 4$ .(a) Find the area of the region  $R$ .  $A = \int_0^4 \sqrt{x} dx = \frac{16}{3}$  or 5.333(b) Find the value of  $h$  such that the vertical line  $x = h$  divides the region  $R$  into two regions of equal area.

$$\int_0^h \sqrt{x} dx = \frac{8}{3} \quad \text{So, } h = \sqrt[3]{16} \approx 2.520 \approx 2.519$$

(c) Find the volume of the solid generated when  $R$  is revolved about the  $x$ -axis.

$$V = \pi \int_0^4 (\sqrt{x})^2 dx = 8\pi \approx 25.133 \approx 25.132$$

(d) The vertical line  $x = k$  divides the region  $R$  into two regions such that when these two regions are revolved about the  $x$ -axis, they generate solids with equal volumes. Find the value of  $k$ .

$$\pi \int_0^k (\sqrt{x})^2 dx = 4\pi$$

$$k = \sqrt{8} \approx 2.828$$